

**SPECIAL RELATIVITY VIOLATES PASCAL'S LAW**

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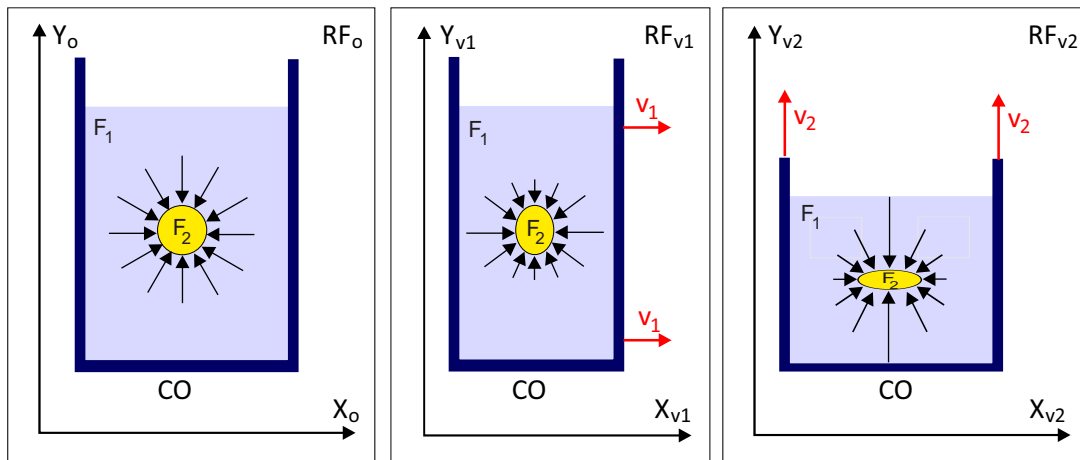
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**Abstract.** The FitzGerald-Lorentz contraction in the direction of relative motion is the starting point of a short and simple argument based on the hydrostatic pressure that formally proves the theory of special relativity violates Pascal's law. From this violation, the formal inconsistency of the theory of special relativity is immediately demonstrated, an inconsistency for which only its second fundamental principle could be responsible.

**Keywords:** Hydrostatic pressure, Pascal Law, special relativity, relativistic length contraction, relativistic time dilation, relativistic phase difference in synchronization, principles of special relativity, speed of light.

**1. Special relativity violates Pascal's law**

Let  $RF_o$ ,  $RF_{v1}$ , and  $RF_{v2}$  be three inertial reference frames whose spacial axes coincide at a certain instant and such that  $RF_o$  moves relative to  $RF_{v1}$  and  $RF_{v2}$  parallel to their respective axes  $X_{v1}$  and  $Y_{v2}$ , and with relative velocities  $v_1$  and  $v_2$ , respectively.  $RF_o$  is the proper reference frame of a container  $CO$  containing a fluid  $F_1$  inside which there is a bubble of another fluid  $F_2$  in static equilibrium with  $F_1$ , because both fluids have the same density and are immiscible. According to Pascal's law, the bubble of  $F_2$  will have a perfect spherical shape, since the same pressure acts on each of its points (Figure 1, left).



**Figure 1** – Left: Fluid bubble  $F_2$  in equilibrium with fluid  $F_1$  in the proper reference frame of both fluids and their container  $CO$ . Center and right: the same container and fluids observed from  $RF_{v1}$  and  $RF_{v2}$ , from whose perspectives  $RF_o$  moves in the direction of  $X_{v1}$  and  $Y_{v2}$  respectively, with velocities  $v_1$  (in the case of  $RF_{v1}$ ) and  $v_2$  (in the case of  $RF_{v2}$ ).

However, according to the Lorentz Transformation, in  $RF_{v1}$  and in  $RF_{v2}$  the bubble will be observed as clearly ellipsoidal in shape, with the minor axis of the respective ellipsoids parallel to the direction of relative motion of  $RF_o$  observed from  $RF_{v1}$  and  $RF_{v2}$ ; and the greater the relative velocity at which  $RF_o$  is observed, the greater the observed narrowing of the fluid bubble  $F_2$  inside the fluid  $F_1$  (Figure 1 center and right). This deformation of the bubble is not due to a differential force acting only on the bubble: all objects in  $RF_o$ , including the fluid container  $CO$  and the two fluids  $F_1$  and  $F_2$ , move at the same relative velocity with respect to any other inertial reference frame in relative motion with respect to  $RF_o$ . The deformations of the bubble  $F_2$  observed in  $RF_{v1}$  and  $RF_{v2}$  (and in any other inertial reference frame moving relative to  $RF_o$ ) are relativistic deformations due exclusively to the FitzGerald-Lorentz contraction.

Therefore, Pascal's law does not hold true in  $RF_{v1}$  or  $RF_{v2}$ , nor in any other inertial reference frame from which  $RF_o$  moves relatively with any non-zero velocity vector. Pascal's law only holds

true in the inertial reference frames of the fluids involved, as in the case of  $RF_o$ . In addition to these violations of Pascal's law, the  $F_2$  bubble cannot simultaneously have different real shapes, as would be the case if the relativistic contraction of physical objects in relative motion that produces them were real and observed simultaneously at different relative velocities.

Consequently, relativistic contractions of space and physical objects observed from inertial reference frames other than the proper reference frame of those objects can only be apparent, and therefore false, as false as the apparent daily rotation of the Sun around the Earth. Thus, if  $L_o$  is the length of any object  $A$  in its proper inertial reference frame  $RF_o$ , it must also be so in any other inertial reference frame  $RF_v$ :  $L_v = L_o, \forall v$ , where  $v$  is the relative velocity between  $RF_v$  and  $RF_o$ .

One could argue that Pascal's law is an exception. But if it were, that exception would have to be explicitly stated in the special theory of relativity, and an explanation would have to be given as to why it is an exception. This is not the case. Furthermore, there are other relativistic violations of other physical laws, such as the laws of reflection [7] and refraction of light [6], or the laws of motion on inclined planes [8].

## 2. Consequences for the theory of special relativity

(This section partially reproduces a text taken from [8])

Let us consider two inertial reference frames  $RF_o$  and  $RF_v$ , whose spatial axes coincide at a certain instant and such that  $RF_o$  moves relative to  $RF_v$  with a uniform velocity  $v$  parallel to the axis  $X_v$  of  $RF_v$ . And let  $S$  be a source of photons at rest in  $RF_o$ . Suppose that  $S$  emits a photon  $a^*$  that travels in  $RF_o$  a distance  $d_o$  to a final screen, which the photon reaches in a time  $t_o$ . The speed of light  $c$  in  $RF_o$  will be:  $c = d_o/t_o$ . According to the Second Principle of Special Relativity, in  $RF_v$  we will have for this photon  $a^*$ :  $c = d_v/t_v = d_o/t_o$ . And since according to the above argument  $d_v = d_o$ , it will also be  $t_v = t_o$ , and then:

$$t_v = \gamma \left( t_o + \frac{d_o v^2}{c^2} \right) = t_o \quad (1)$$

which is only possible if  $v = 0$  and consequently  $\gamma = 1$ . Therefore, the only valid measurements of space and time are those made in the proper inertial reference frames of the objects involved. Those made in other inertial reference frames can only be apparent, and therefore false, as false as the apparent refractive distortions of physical objects partially submerged in water.

The theory of special relativity is, therefore, an inconsistent theory. And the reason for its inconsistency cannot be the first of its fundamental principles, which establishes the universality of physical laws, because if that principle were false, the consistent evolution of the universe, for which there is overwhelming empirical evidence, would be impossible. It must therefore be the second of its fundamental principles, a principle that establishes that the speed of light is always the same for all inertial reference frames, regardless of the speed of these inertial reference frames with respect to the light source. The speed of light would always be the same, but THROUGH THE ABSOLUTE REAL PHYSICAL SPACE in which it propagates.

Even if only one of the falsehoods that have just been proven is sufficient to establish both the inconsistent nature of the theory of special relativity and the formal cause of that inconsistency (its second fundamental principle), this last paragraph is included to justify why neither the relativistic increase in mass with velocity nor the relationship between mass and energy has been discussed. The reason is that both results can be formally deduced outside of theory of special relativity [10], [4], [1], [9],[5] [2], [3].

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